

Honors Algebra 2

Solving Quadratic Equations Using Non-Factoring Methods

Name _____

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I. Solving Quadratic Equations using Inverse Operations

The two types of equations we can solve using inverse operations generally look like:

$$ax^2 + c = 0 \quad \text{or} \quad a(x-h)^2 + k = 0$$

- $ax^2 + bx + c = 0$
- 1. IO
 - 2. Factor
 - 3. CS
 - 4. QF

How to Solve a Quadratic Equation using Inverse Operations

1. **Isolate the variable or expression** that is being squared by using inverse operations.
2. Undo the square by using the inverse operation - a square root. This step will always produce positive and negative roots so use \pm .
3. Continue solving for x if needed using inverse operations. Simplify the radical as much as possible and combine like terms if needed.

Please note: In this unit we will find real and imaginary solutions. A quadratic equation always has 2 solutions; 2 real, 2 imaginary, or 1 real, repeated solution. What type of quadratic equation gives a repeated solutions?

Perfect Square Trinomial

$$x^2 + 14x + 49 = 0$$

$$(x+7)(x+7) = 0$$

$$\sqrt{(x+7)^2} = \pm \sqrt{0}$$

$$x+7 = 0$$

$$x = -7$$

mult. 2

Solve the equation using inverse operations. Write the answer in simplest form (no decimals).

1. $x^2 + 16 = 0$

$$\begin{array}{r} -16 \quad -16 \\ \hline \sqrt{x^2} = \pm \sqrt{-16} \\ \boxed{x = \pm 4i} \end{array}$$

2 Imaginary
Complex conjugates

2. $7x^2 + 207 = 4x^2 + 300$

$$\begin{array}{r} -4x^2 \quad -4x^2 \\ \hline 3x^2 + 207 = 300 \\ \underline{-207} \quad \underline{-207} \\ 3x^2 = 93 \\ \hline \frac{3x^2}{3} = \frac{93}{3} \\ \sqrt{x^2} = \pm \sqrt{31} \\ \boxed{x = \pm \sqrt{31}} \end{array}$$

2 irrational solutions
radical conjugates
 $a \pm \sqrt{b}$

3. $(x+2)^2 + 49 = 0$

$$\begin{array}{r} -49 \quad -49 \\ \hline \sqrt{(x+2)^2} = \pm \sqrt{-49} \\ x+2 = \pm 7i \\ \underline{-2} \quad \underline{-2} \\ \boxed{x = -2 \pm 7i} \\ x = -2 - 7i, -2 + 7i \end{array}$$

4. $\frac{2}{3}(x+8)^2 - 6 = 0$

$$\begin{array}{r} +6 \quad +6 \\ \hline \frac{2}{3} \cdot \frac{3}{2} (x+8)^2 = \frac{6}{1} \left(\frac{3}{2}\right) \\ \sqrt{(x+8)^2} = \sqrt{9} \\ x+8 = \pm 3 \\ x = -8 \pm 3 \\ x = -8 + 3 = -5 \\ x = -8 - 3 = -11 \end{array}$$

$x = -5, -11$

| | |
|---|--|
| <p>5. $x^2 + 14 = -22$</p> $\pm \sqrt{x^2 \pm \frac{-14}{1} \pm \frac{-14}{1}}$ $\pm \sqrt{x^2 \pm \sqrt{-36}}$ <p>$x = \pm 6i$</p> | <p>6. $2x^2 - 5 = 5x^2 + 37$</p> $2x^2 - 42 = 5x^2$ $-42 = 3x^2$ $\pm \sqrt{-14} = \sqrt{x^2}$ <p>$x = \pm \sqrt{14}i$</p> |
| <p>7. $\frac{1}{4}(x-5)^2 = 16$</p> $\frac{1}{4} \cdot \frac{4}{1} (x-5)^2 = 16 \cdot \frac{4}{1}$ $\sqrt{(x-5)^2} = \pm \sqrt{64}$ $x-5 = \pm 8$ $x = 5+8$ $5-8$ <p>$x = 13, -3$</p> | <p>8. $-(x+9)^2 = -12$</p> $\sqrt{(x+9)^2} = \pm \sqrt{12}$ $x+9 = \pm \sqrt{12}$ <p>$x = -9 \pm 2\sqrt{3}$</p> |

Additional Practice: Show all work and check you answer (below).

9. $7x^2 + 16 = 9x^2 - 20$

10. $2(x+2)^2 + 72 = 0$

11. $(4x-5)^2 - 14 = 50$

12. $6x^2 + 65 = x^2 + 5$

Solutions

9. $x = \pm 3\sqrt{2}$

10. $x = -2 \pm 6i$

11. $x = -\frac{3}{4}, \frac{13}{4}$

12. $x = \pm 2i\sqrt{3}$