

Calculator use is allowed; you may not use a calculator with matrix operations. Show all work and write your answer on the line!

1. Use substitution to solve the system of equations.

$$\begin{aligned}x + 2y - z &= -3 \\ -2x + y - 3z &= -9 \\ y &= -2z + 3\end{aligned}$$

$$\begin{aligned}\textcircled{1} \quad x + 2(-2z + 3) - z &= -3 \\ x - 4z + 6 - z &= -3\end{aligned}$$

$$x - 5z = -9$$

$$\begin{aligned}\textcircled{2} \quad -2x - 2z + 3 - 3z &= -9 \\ -2x - 5z &= -12\end{aligned}$$

$$\begin{aligned}\textcircled{3} \quad x - 5z &= -9 \\ -2x - 5z &= -12 \\ \hline -x + 5z &= 9 \\ \hline -3x &= -3 \\ x &= 1\end{aligned}$$

$$\begin{aligned}\textcircled{4} \quad 1 - 5z &= -9 \\ -5z &= -10 \\ z &= 2\end{aligned}$$

$$\begin{aligned}\textcircled{5} \quad y &= -2(2) + 3 \\ &= -1\end{aligned}$$

Answer: _____ $(1, -1, 2)$

2. Solve using elimination.

$$\begin{array}{l} x + y - z = 11 \\ 2x + 2y - 3z = 28 \\ 4x - y + 5z = -20 \end{array}$$

$$\begin{array}{l} \textcircled{1} \quad 2x + 2y - 3z = 28 \\ \quad -2x - 2y + 2z = -22 \\ \quad \quad -z = 6 \\ \quad \quad z = -6 \end{array}$$

$$\begin{array}{l} \textcircled{2} \quad x + y - z = 11 \\ \quad 4x - y + 5z = -20 \\ \quad \quad 5x + 4z = -9 \end{array}$$

$$\begin{array}{l} \textcircled{3} \quad 5x + 4z = -9 \\ \quad 5x + 4(-6) = -9 \\ \quad \quad 5x = -9 + 24 \\ \quad \quad 5x = 15 \\ \quad \quad x = 3 \end{array}$$

$$\begin{array}{l} \textcircled{4} \quad 3 + y + 6 = 11 \\ \quad \quad y = 2 \end{array}$$

Answer: (3, 2, -6)

Calculator use is allowed; you may not use a calculator with matrix operations. Show all work and write your answer as an ordered-triple on the line!

1. Use elimination to solve the system of equations.

$$\begin{aligned}x + y - z &= 14 \\2x + 2y - 3z &= 35 \\4x - y + 5z &= -22\end{aligned}$$

$$\begin{aligned}\textcircled{1} \quad x + y - z &= 14 \\4x - y + 5z &= -22\end{aligned}$$

$$5x + 4z = -8$$

$$\begin{aligned}\textcircled{2} \quad -2x - 2y + 2z &= -28 \\2x + 2y - 3z &= 35 \\-z &= 7 \\z &= -7\end{aligned}$$

$$\begin{aligned}\textcircled{3} \quad 5x + 4(-7) &= -8 \\5x &= -8 + 28 \\5x &= 20 \\x &= 4\end{aligned}$$

$$\begin{aligned}\textcircled{4} \quad 4 + y + 7 &= 14 \\y &= 3\end{aligned}$$

Answer: (4, 3, -7)

2. Use substitution to solve the system of equations.

CBA
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$$\begin{aligned}x + 2y - z &= 5 \\ -2x + y - 3z &= 0 \\ y &= -2z - 1\end{aligned}$$

$$\textcircled{1} \quad x + 2(-2z - 1) - z = 5$$

$$x - 4z - 2 - z = 5$$

$$x - 5z = 7$$

$$\textcircled{2} \quad -2x - 2z - 1 - 3z = 0$$

$$-2x - 5z = 1$$

$$\textcircled{3} \quad \begin{aligned}2(x - 5z) &= 7(2) \\ -2x - 5z &= 1\end{aligned}$$

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$$2x - 10z = 14$$

$$\underline{\quad\quad\quad} \quad -15z = 15 \rightarrow z = -1$$

$$\textcircled{3} \quad x + 5(-1) = 7$$

$$x + 5 = 7 \rightarrow x = 2$$

$$\textcircled{4} \quad y = -2(-1) - 1$$

$$y = 1$$

Answer: (2, 1, -1)